

Sampling

Fourier Transformation

$$f(x) = \int_{-\infty}^{\infty} F(\omega) e^{2\pi i \omega x} d\omega$$

$$F(\omega) = \int_{-\infty}^{\infty} f(x) e^{-2\pi i \omega x} dx$$

Sinus Cardinalis (sinc)

$$\text{sinc}(x) = \frac{\sin(\pi x)}{\pi x}$$

Texturing

Summed Area Table

$$S(u_0, v_0) = \sum T(u, v) \quad u \leq u_0, v \leq v_0$$

Mip-Mapping

$$D = \text{ld}(\max(d_1, d_2))$$

D Level

d₁, d₂ Diagonalen

Filterung (MipMapping)

$$T_0 := \text{Wert von } D_0 = \text{trunc}(D) \quad \text{bilineare Int.}$$

$$T_1 := \text{Wert von } D_1 = D_0 + 1 \quad \text{trilineare Int.}$$

$$\text{Pixel} = (D_1 - D) \cdot T_0 + (D - D_0) \cdot T_1$$

Kurven

Bezier-Kurven (de Casteljau)

$$b_i^r := (1-t)b_i^{r-1} + tb_{i+1}^{r-1} \quad b_0^1 := b_i$$

Bezier-Kurve

$$b(t) = \sum_{i=0}^n b_i B_i^n(t)$$

Bernstein-Polynom (f. Bezier)

$$B_i^n(t) = \binom{n}{i} (1-t)^{n-i} t^i$$

B-Spline

$$s(u) = \sum_{i=0}^n d_i N_i^k(u) \quad (k = \text{Ordnung})$$

NURBS

$$n(u) = \frac{\sum_{i=0}^n \omega_i d_i N_i^k(u)}{\sum_{i=0}^n \omega_i N_i^n(u)} \quad \omega = \text{Gewicht}$$

Advanced Modelling

Blobby Objects

$$f(x, y, z) = \sum_k b_k e^{-a_k r_k^2} - T = 0$$

$$r_k^2 = x_k^2 + y_k^2 + z_k^2$$

a, b Faktoren für die Blobbiness

T Treshold

Superellipsen (2D)

$$\left(\frac{x}{r_x}\right)^{\frac{2}{s}} + \left(\frac{y}{r_y}\right)^{\frac{2}{s}} = 1$$

$$x = r_x \cos^s \kappa$$

$$y = r_y \sin^s \kappa$$

$$-\pi \leq \kappa \leq \pi$$

Superellipsoid (3D)

$$\left[\left(\frac{x}{r_x}\right)^{\frac{2}{s_2}} + \left(\frac{y}{r_y}\right)^{\frac{2}{s_2}} \right]^{\frac{s_2}{s_1}} + \left(\frac{z}{r_z}\right)^{\frac{2}{s_1}} = 1$$