

Dependable Systems - Lab Report

NAME Name

Version 1.1
2024-07-02

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1 Exercise 2a - Fault-Tolerant Computer System

The Model should have these properties:

1. A fault-tolerant computer system consist of two main CPUs.
2. The fault-tolerant computer system tolerates the failure of any one of the main CPUs. I.e., as long as only one main CPU fails, the system remains operational.
3. Failure rate = $1/1000$; Repair rate = $1/10$

I modeled the states as follows:

s=0	The system is fully functional.
s=1	One CPU has failed, the system is still running.
s=2	Both CPUs have failed, the system is down.

I implemented this in 2a_computerSystem.pm:

```
1 ctmc
2
3 //definition of the failure rate
4 const double rate_failure = 1/1000;
5 const double rate_repair = 1/10;
6 module PC
7     //definition of states
8     s: [0..2] init 0;
9     //guard -> rate: action;
10    [] s=0 -> rate_failure*2: (s'=1);
11    [] s=1 -> rate_repair: (s'=0);
12    [] s=1 -> rate_failure: (s'=2);
13    [] s=2 -> rate_repair*2: (s'=1);
14 endmodule
15
16 //definiton of the reward system
17 rewards
18     s=0: 1;
19     s=1: 1;
20 endrewards
```

To calculate the MTTF and the availability of the system I used query2a.pct1:

```
1 //mttf
2 R=? [ F(s=2) ]
3 //Result: 51494.764692749566 (+/- 0.5132659280373123 estimated; rel err
4     9.967341944366238E-6)
5
6 //availability
7 S=? [ !(s=2) ]
8 //Result: 0.9999019703872098
```

I got the results with this command: `./prism 2a_computerSystem.pm query2a.pct1 -sor`

1.1 Plotting reliability

I used the script bellow to get some values for the reliability of the system and plotted it with latex.

```
1 #!/bin/bash
2
3 outfile=result_2a_v2.csv
4 #ensure the output file is empty
5 echo "Time,Reliability" > $outfile
6
7 for t in $(seq 0 2000 50000)
8 do
9     #create query
10    echo "P=? [ !(F[0, $t] s=2) ]" > help.pctl
11    result=$(./prism 2a_computerSystem.pm help.pctl | grep -oP '(?<=
12        Result: )[^ ]+')
13    #save the result to the CSV file
14    echo "$t,$result" >> $outfile
done
```

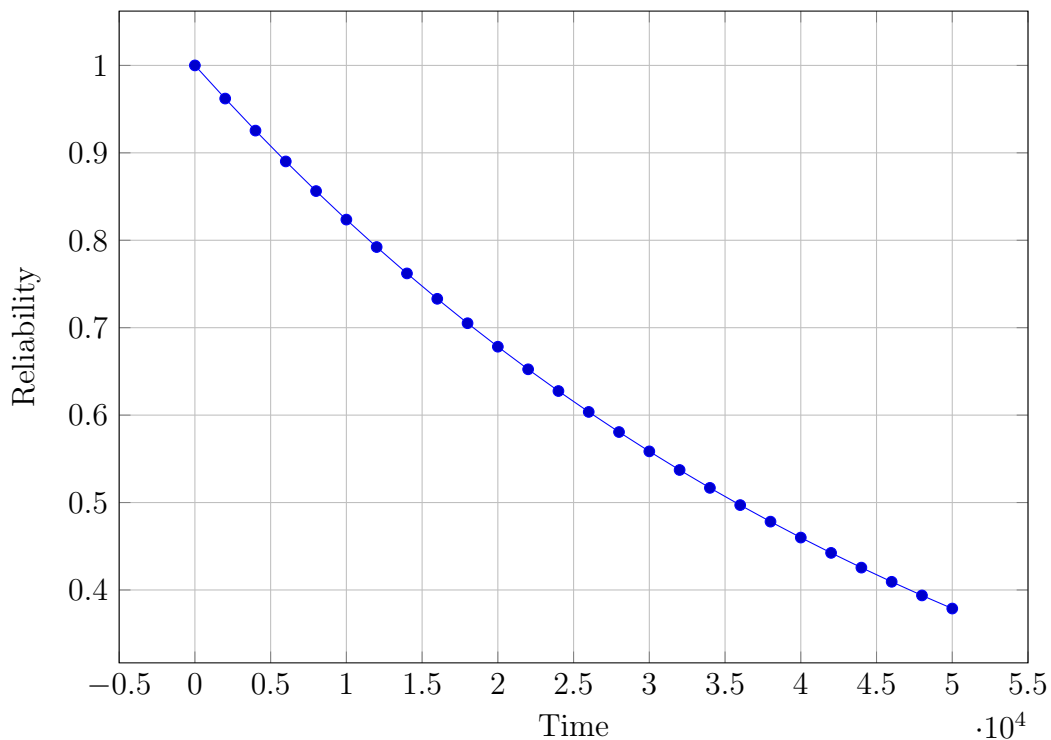


Abbildung 1: Reliability over Time

2 Exercise 2b - Fault-Tolerant Computer System

The Model should have these properties:

1. A fault-tolerant computer system consist of two main CPUs.

2. The fault-tolerant computer system tolerates the failure of any one of the main CPUs. I.e., as long as only one main CPU fails, the system remains operational.
3. Failure rate = 100 FIT; Repair rate = none
4. Assumption Coverage = 0.7

I modeled the states as follows:

s=0	The system is fully functional.
s=1	One CPU has failed (with our assumed fail behavior), the system is still running.
s=2	The system is not operational.

Our new failure rate:

$$1 \text{ FIT} = 10^{-9} \frac{\text{failures}}{\text{hour}}$$

$$100 \text{ FIT} = 100 \cdot 10^{-9}$$

I implemented this in 2b.pm:

```

1 ctmc
2
3 //definition of the failure rate
4 const double rate_failure = 100 * 1e-9;
5 const double coverage = 0.7;
6 module PC
7     //definition of states
8     s: [0..2] init 0;
9     //guard -> rate: action;
10    [] s=0 -> rate_failure*2*coverage: (s'=1); //good failure
11    [] s=0 -> rate_failure*2*(1-coverage): (s'=2); //bad failure
12    [] s=1 -> rate_failure: (s'=2);
13 endmodule
14
15 //definiton of the reward system
16 rewards
17     s=0: 1;
18     s=1: 1;
19 endrewards

```

To calculate the MTTF and the availability of the system I used query2b.pctl:

```

1 //mttf
2 R=? [ F(s=2) ]
3 //Result: 1.2E7 (exact floating point)
4
5 //availabilty
6 S=? [ !(s=2) ]
7 //Result: 0.0

```

I got the results with this command: `./prism 2b.pm query2b.pctl`

2.1 Plotting reliability

I used the script bellow to get some values for the reliability of the system and plotted it with latex.

```
1 #!/bin/bash
2
3 outfile=result_2b.csv
4 #ensure the output file is empty
5 echo "Time,Reliability" > $outfile
6
7 for t in $(seq 0 200000 5000000)
8 do
9     #create query
10    echo "P=? [ !(F[0, $t] s=2) ]" > help.pctl
11    result=$(./prism 2b.pm help.pctl | grep -oP '(?<=Result: )[^ ]+')
12    #save the result to the CSV file
13    echo "$t,$result" >> $outfile
14 done
```

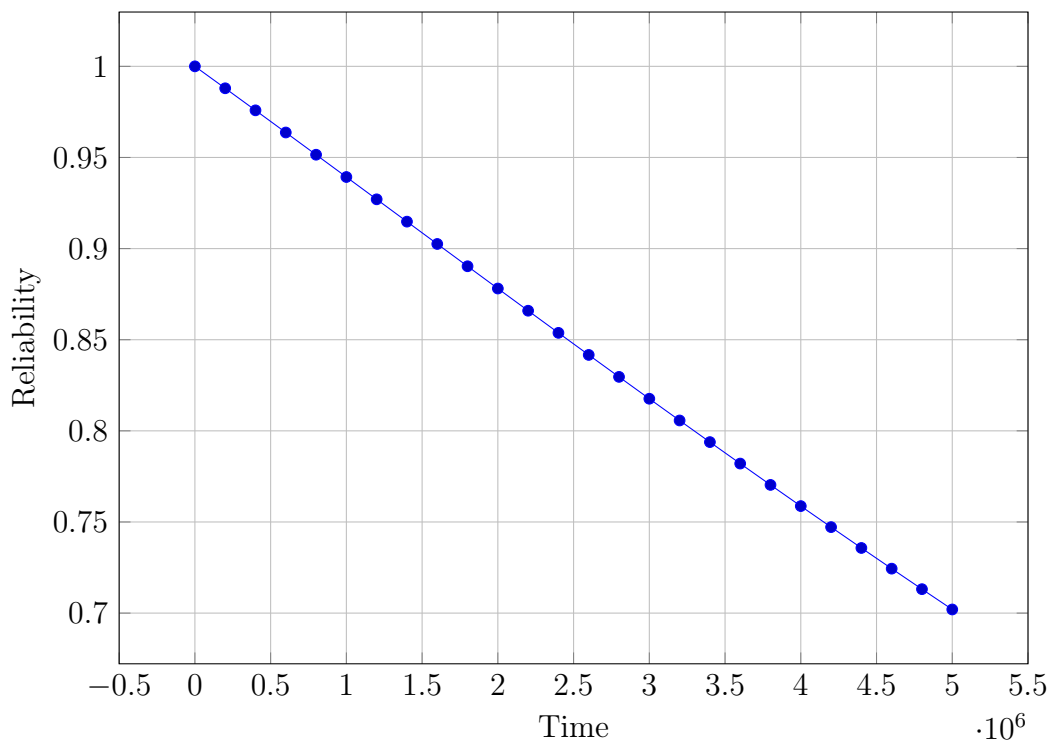


Abbildung 2: Reliability over Time

3 Exercise 3 - Your turn!

My model describes a person and their relationship status:

1. in a relationship (good state):

- (a) normal fights decrease the quality of the relationship (relationship component failure)
 - (b) there can be fights that destroy the relationship (not covered relationship component failure)
 - (c) talking can make the relationship better (relationship repair)
 - (d) if the relationship quality is too bad it is broken (relationship failure)
2. if not in a relationship, they can find a (new) relationship (repair)
 3. can get depressed and not be able to find a new relationship (full system failure)

I modeled this with those states:

$s > 0$	in a relationship, how good the relationship is depends on the value of s
$s = 0$	currently alone
$s = -1$	depressed and therefore not able to find a new relationship

An implementation of this system can be seen in 3.pm:

```

1  ctmc
2
3  //definitions of rates
4  const double fights = 1/96;      //fight rate (1/(4 days))
5  const double c_fights = 0.999;  //coverage for fights
6  const double talk = 1/24;       //relationship talk rate
7  const int states = 8;           //quality levels of a relationship
8  const double new = 1/9000;      //rate of finding a new relationship (~1 y)
9  const int start_new = floor(states/2);
10 const double dep = 1/35000;     //rate of depression if alone (~1/(4y))
11 module Person
12     //definition of states
13     s: [-1..states] init start_new;
14     //guard -> rate: action;
15     [] s > 0 -> fights*c_fights: (s'= s-1);           //good failure
16     [] s > 0 -> fights*(1-c_fights): (s'= 0);         //bad failure
17     [] s > 0 & s < states -> talk : (s'= s+1);
18     [] s = 0 -> new : (s'= start_new);
19     [] s = 0 -> dep : (s'= -1);
20     [] s = -1 -> 1 : (s'= -1);
21 endmodule
22
23 //definiton of the reward system
24 rewards
25     s > 0: 1;
26 endrewards

```

To calculate the MTTF and the availability of the system I used query3.pctl:

```

1 //mttf
2 R=? [ F(s=0) ]
3 //Result: 92377.90895729311 (+/- 0.9232281743199776 estimated; rel err
4     9.994036287905064E-6)
5 // (around 10.5 years)

```

```

6 //availability
7 S=? [ !(s=0 & s=-1) ]
8 //Result: 1.0

```

I used this command to get the results: `./prism 3.pm query3.pctl -maxiters 100000 -sor`

3.1 Plotting reliability

I used the script bellow to get some values for the reliability of the system and plotted it with latex.

```

1 #!/bin/bash
2
3 outfile=result_3.csv
4 #ensure the output file is empty
5 echo "Time,Reliability" > $outfile
6
7 for t in $(seq 0 5000 100000)
8 do
9     #create query
10    echo "P=? [ !(F[0, $t] s=2) ]" > help.pctl
11    result=$(./prism 3.pm help.pctl | grep -oP '(?<=Result: )[^ ]+')
12    #save the result to the CSV file
13    echo "$t,$result" >> $outfile
14 done

```

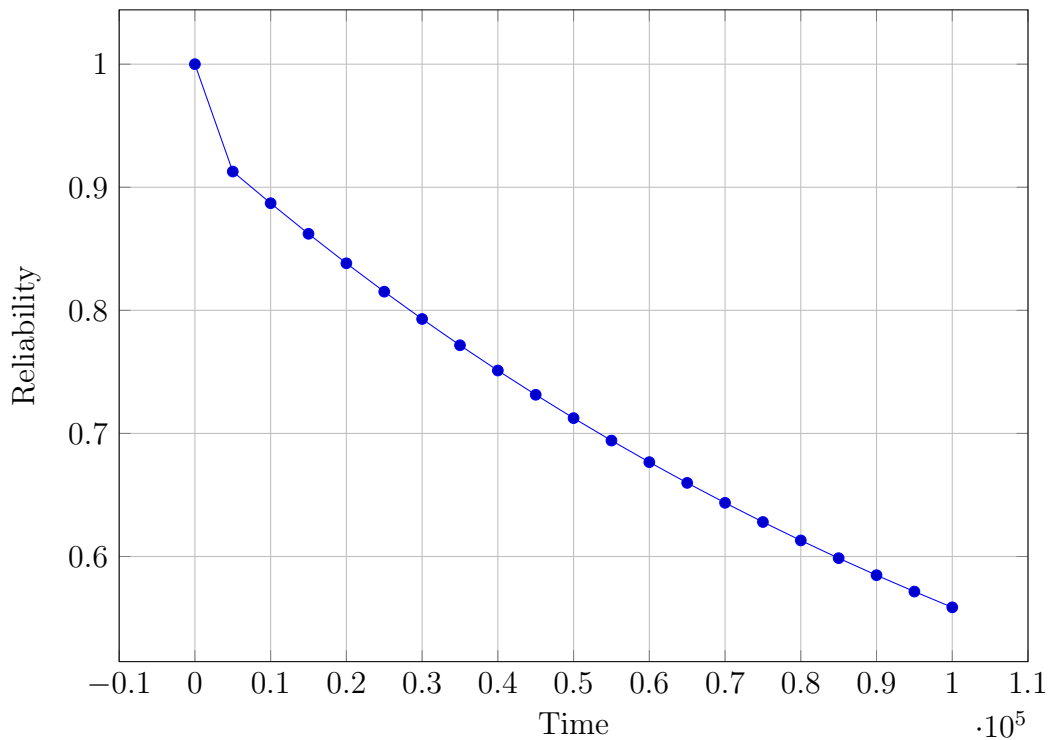


Abbildung 3: Reliability over Time