

## Disclaimer

Das ist nur eine Zusammenfassung und kein Ersatz für das Skriptum / die VOs. Keine Garantie darauf, dass alles so stimmt, wie es hier steht. Das ist nur meine Interpretation der Inhalte. Falls etwas unklar sein sollte, bitte im Skriptum nachschauen.

(meines Verständnisses nach)

Second Block ist nicht inkludiert, da dieser nicht Teil vom Prüfungsstoff ist.



ERFOLG

BETEN

Viel Spaß beim Lernen!

(und viel Glück beim Test)

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## 1. Block: "Shared Memory" Systeme

↳ less accesses to (slow) main memory needed

Cache = small, fast memory  $\Rightarrow$  reduces access times by reusing read values, create overhead if no reuse

↳ segmented in blocks (typically of 64 Bytes size), granularity: unit of memory blocks

↳ cache line: stores one memory block + meta information (bits, flags)

↳ direct mapping: map each block on predetermined line; fully associative: map block on any cache line

set associative: map each block on any line within predetermined set; k-way set associative: k-set sizes  $k=2, 4, 8, \dots$

is block that contains read word in the cache? yes = cache hit  $\Rightarrow$  fast read / no = cache miss  $\Rightarrow$  read block into c.line

compulsory (cold) miss: empty cache, contains no address blocks

usually least recently

capacity miss: full cache, some cache line has to be evicted or least frequently used (LRU/LFU),

conflict miss: full set, frequent in directly mapped caches, either of k lines can be evicted  $\Rightarrow$  eviction policy

is block of the address written to in the cache? yes = overwrite it / no = allocate or update address in memory  $\rightsquigarrow$  write, no-allocate

write through: update block that is in cache line by writing value to memory

write back: keep value in cache line until it is evicted

types of locality of access: temporal locality - several reuses of memory address contents in brief succession

spatial locality - several reuses of memory addresses in same block

READ

WRITE

## MCC PROBLEMS

Work/Seq. Time of Matrix-Matrix Multiplication Algorithm:  $O(nml)$   
miss-rate determined by line size,  
Factor of 20-40 between best and worst loop orders because of row-major storage in C  $\Rightarrow$  cache stores 1 row  
Work of recursive, divide-and-conquer Matrix-Matrix Multiplication Algorithm:  $O(\log^2 n)$  or even  $O(n^{2.81})$   
Cache-Aware Algorithm: small enough submatrices to fit in the cache/cache oblivious: everything above

Multi-Core Caches: Hierarchy of Caches in increasing Size ( $L_1$ =lowest level, fastest, smallest, closest to CPU)  
 $\hookrightarrow L_1$ : usually divided into data and instruction caches  $\Rightarrow$  has another cache: translation look-aside buffer (TLB)  
 $\hookrightarrow L_1$  and sometimes  $L_2$ : private to one processor-core, as opposed to shared higher-level caches  
cache coherence problem: memory block is in private  $L_1$  cache of two cores  
coherent cache system: cache line gets updated in both / non-coherent cache system: it never gets updated in both  
updated = modified with the new value or invalidated (= next access is a miss)  
non-trivial task, requires cache coherence protocol, fulfills local consistency, update transfer & write consistency  
false sharing problem: caused by granularity  $\Rightarrow$  updates to two addresses by two cores create coherence traffic  
 $\hookrightarrow$  avoided by allocating frequently used variables on different cache lines (e.g. padding = one address per block)

write buffer: buffers writes to the main memory to process them in the appropriate pace, makes them appear fast  
may be FIFO or sorted, usually coalesce writes to same address, NUMA to the main memory

memory controller: ensures connection between CPU core and main memory, memory is banked along the controller  
access times per core depend on "closeness" to controller

"first touch" policy: virtual memory page will be put in the memory bank closest to the core  $\Rightarrow$  performance boost

super-linear speed-up: working set on  $p$  processors  $\Rightarrow \frac{1}{p}$  of the working set on one processor  
if  $p$  grows  $\Rightarrow \frac{1}{p}$  shrinks and fits in faster caches  $\Rightarrow$  speed-up of  $k p$ ,  $k > 1$

roofline performance model: distinction between memory-bound and compute-bound applications:

memory-bound app: operations performed per unit read/write take less time than reading/writing a unit  
 $\hookrightarrow$  memory performance (= access times) determines system performance

compute-bound app: operations performed per unit read/write take more time than reading/writing a unit  
 $\hookrightarrow$  nominal processor performance determines system performance

programm order: seq. execution  $\Rightarrow$  reads/writes happen in execution order of the program's instructions

$\hookrightarrow$  proves properties of state invariants  
 $\hookrightarrow$  concurrent, asynchronous execution of two programs  $\Rightarrow$  interleaving necessary to ensure memory = program order

sequential consistency: type of memory consistency, considers possibility of different interleavings

$\hookrightarrow$  not fulfilled in modern multi-core systems, due to per-core write buffers

$\hookrightarrow$  well-defined memory state gets ensured by hardware mechanisms (memory fences, atomic operations) instead

main problems of MCC: cache coherence - Different Cores write/read Same Memory Address  
memory consistency - Different Cores write/read Different Memory Addresses

### 3. Block: Die Schnittstelle/Sprache OpenMP

Open Multi Processing

- main characteristics:
1. implicit parallelism through work sharing, **SPMD** { all threads execute same program }
  2. Fork join parallelism (master spawns threads, join at the end of parallel area)
  3. unique int thread id per parallel area, consecutively numbered
  4. number of threads can exceed CPU number
  5. Constructs for sharing work across threads
  6. Threads can share variables and have private variables
  7. Unprotected, parallel updates may lead to data races and errors
  8. Synchronisation Constructs for preventing data races
  9. Consistent memory state after Synchronisation

requirements in C: OpenMP-capable compiler, function prototype header (omp.h), "omp\_" prefix on all functions and predefined objects, "OMP\_" prefix for special variables

parallel region construct: structured C statement, once started, number of threads in parallel region unchangeable  
 joining threads through barrier synchronisation, only master remains active after join  
 control of thread number by runtime environment or by num\_threads()  
 ↳ if runt. env.: default value (CPU number) or env. variable OMP\_NUM\_THREADS

oversubscription: set OMP\_NUM\_THREADS larger than CPU amount ⇒ useful for debugging, not performance

openmp library calls: access to stable timer

double omp\_get\_wtime(void); returns wall clock time in s  
 double omp\_get\_wtick(void); returns resolution of the timer

```
int omp_get_thread_num(void);
int omp_get_num_threads(void);
int omp_get_max_threads(void);
void omp_set_num_threads(int num_threads);
```

thread safe - can be called concurrently, in parallel without risk of interference

declaring variables: best practice to set everything to default(None) and manually share everything

private(<comma separated list of variables>) - not initialized  
 firstprivate(<comma separated list of variables>) - initialized to value  
 shared(<comma separated list of variables>) before parallel region  
 default(shared|none) - share variables declared by master by default  
 necessary, shared variables can be read concurrently, but the same variable must not be read & written to at the same time

work sharing:

```
#pragma omp parallel
{
    int i; // private i for each thread
    ...
#pragma omp master
    readdata(a,n);
#pragma omp barrier
    // compute
    for (i=0; i<n; i++) {
        b[i] = ...; // per thread computation from a into b
    }
    #pragma omp barrier - no thread may continue before all threads have reached this point
    #pragma omp single nowait
    writedata(b,n);
}

#pragma omp sections [clauses]
<section block>
#pragma omp section [clauses]
<structured statement>
#pragma omp for [clauses] for (<canonical form loop range>)
<loop body>
#pragma omp parallel for [clauses] - does not allow nowait
```

#pragma omp master - all threads skip it except master  
 <structured statement> - no mutual exclusion necessary

#pragma omp private / firstprivate can cause data races

#pragma omp single [clauses] done by either of the threads  
 <structured statement> - has implied barrier at the end ⇒ canceled by nowait clause

} no implicit barrier of single construct needed ⇒ eliminated by nowait because there already is a barrier, no correctness guaranteed without it ⇒ data races in both a and b possible

consists of:

} ends with barrier ⇒ canceled by nowait while-loops not one thread pre-assigned per section allowed

⇒ all threads must compute the same, finite loop range and loop range may not change

⇒ canonical form: upper bound must be of the form

i<n, i≤n, i>n, i≥n or i≠n; increment must be of form i++ , i+=inc or i=i+inc (e.g. i-- for decrements)

independence of loops: loop does array updates only; updates at most one unchanged element per iteration

## Loop FUNCTIONS

- Loop scheduling:** how to share loop work through threads?  $\Rightarrow$  loop range is divided into chunks
- ↳ static schedule — same-sized chunks, assigned in static, round-robin fashion
  - ↳ dynamic schedule — same-sized chunks, each thread grabs next unassigned once finished
  - ↳ guided schedule — no fixed size, chunks get assigned dynamically to free threads
- no overhead, fast assignments  
good for same work per iteration  
preferable for loops with index-depending conditions

<code>schedule(static[, chunksize])</code> <code>schedule(dynamic[, chunksize])</code> <code>schedule(guided[, chunksize])</code>	- default chunksize: $\frac{n}{p}$ - default chunksize: 1 - default chunksize: 1	<code>schedule(auto)</code> <code>schedule(runtime)</code> ↳ set in env.var: OMP_SCHEDULE
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### collapse nested loops:

- performance boost
- easier parallelisation

```
#pragma omp parallel for collapse(2) nesting depth to collapse
for (i=0; i<n; i++) { // OpenMP will make one loop out of two
  for (j=0; j<m; j++) {
    x[i][j] = f(i, j);
  }
}
```

### reduction:

```
reduction(<reduction operator>:<reduction variables>) allowed operators: +, -, *, &, |, ^, &&, ||, min, max
#pragma omp scan exclusive(<reduction variables>) for exclusive prefix sums
#pragma omp scan inclusive(<reduction variables>) for inclusive prefix sums
```

### work sharing - part II (tasks): gets completed at latest as possible;

```
#pragma omp task [clauses]
<structured statement>
```

```
#pragma omp taskwait [clauses]
```

### mutual-exclusion constructs:

```
#pragma omp critical [(name)]
<structured statement>
```

```
#pragma omp atomic [read|write|update|capture]
<atomic statement>
```

### Locks:

```
void omp_init_lock(omp_lock_t *lock);
void omp_init_nest_lock(omp_nest_lock_t *lock);
void omp_destroy_lock(omp_lock_t *lock);
void omp_destroy_nest_lock(omp_nest_lock_t *lock);
void omp_set_lock(omp_lock_t *lock);
void omp_set_nest_lock(omp_nest_lock_t *lock);
void omp_unset_lock(omp_lock_t *lock);
void omp_unset_nest_lock(omp_nest_lock_t *lock);
```

### special loops executed with SIMD instructions:

```
#pragma omp simd [clauses]
for (<canonical form loop range>
<loop body>
```

sequential - one thread

```
#pragma omp for simd [clauses]
for (<canonical form loop range>
<loop body>
```

loop within parallel region  
to be shared among threads

```
#pragma omp parallel for simd [clauses]
for (<canonical form loop range>
<loop body>
```

parallel region with  
SIMD loop sharing

```
#pragma omp taskloop [clauses]
for (<canonical form loop range>
<loop body>
```

break iteration range into  
smaller tasks - initiated by single thread

### parallelise loops with hopeless dependencies: by executing non-parallelisable part sequentially

```
#pragma omp ordered
<structured statement>
```

- one ordered block per loop
- brings overhead, allows partial parallelisation

### cilk: gives rise to fully strict computations

```
cilk_spawn <function call> - generate task
cilk_sync same as taskloop
cilk_for (<canonical form iteration space>) <loop body>
```

=> allows merging problem to be solved work-optimally  
with  $T_1(n) = O(n)$  and  $T_{\infty}(n) = O(\log^2 n)$