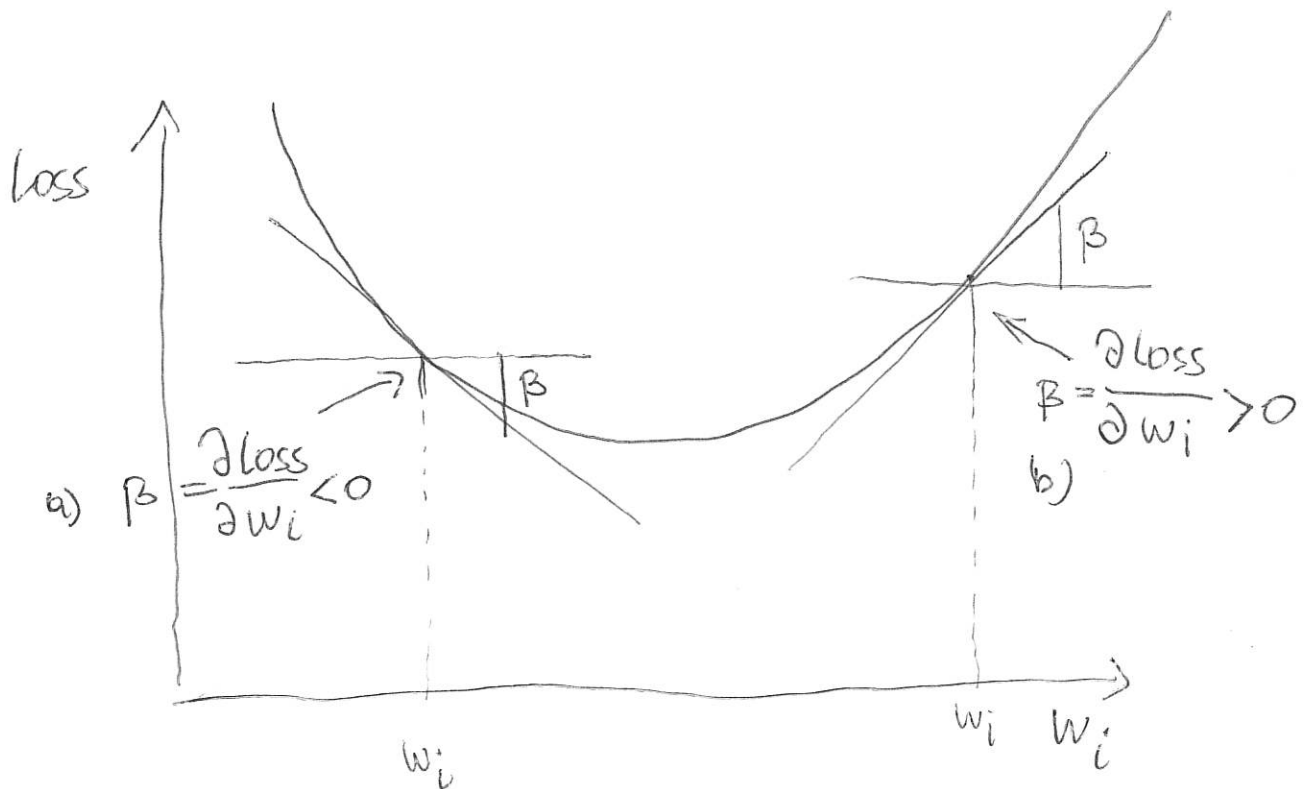


Perceptron Learning

$$h_w(\vec{x}) = g(in), \quad in = \sum_i w_i x_i$$

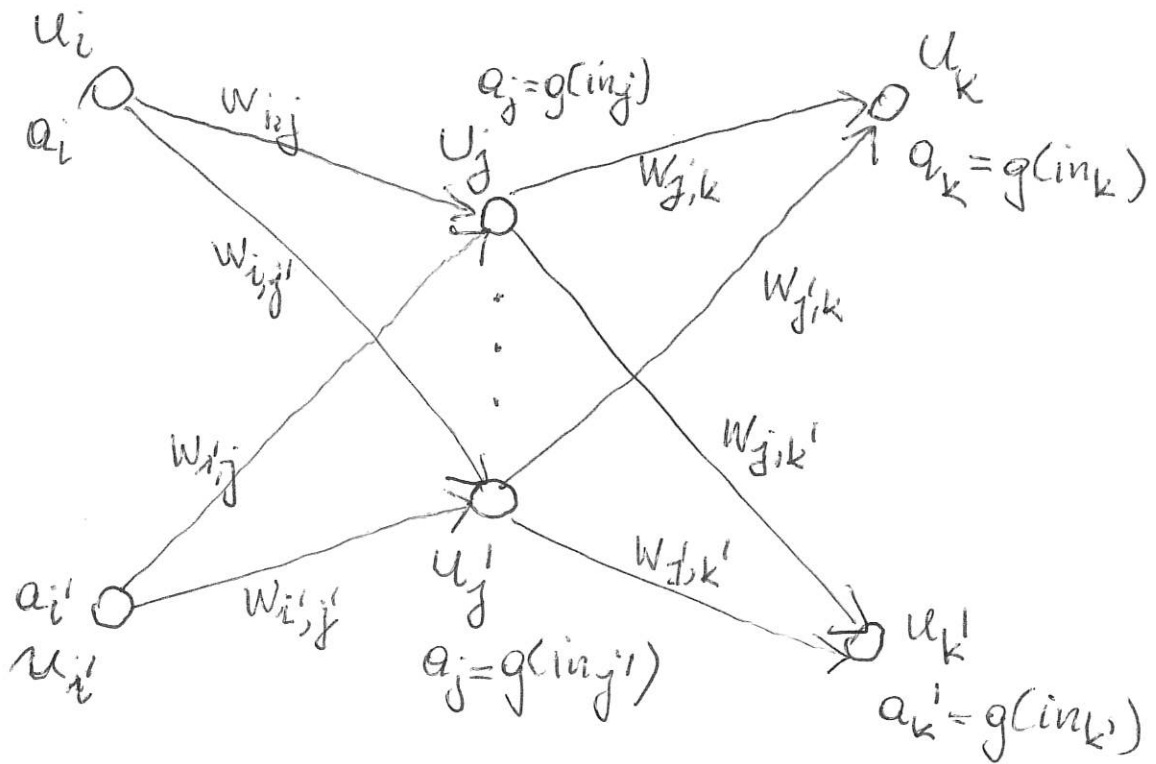
$$\text{Loss}(w) = \text{Err}^2 = (y - h_w(x))^2$$



a) increase w_i by β to affect $g(in)$

b) decrease w_i by β to affect $g(in)$

Multi-Layer Perceptrons



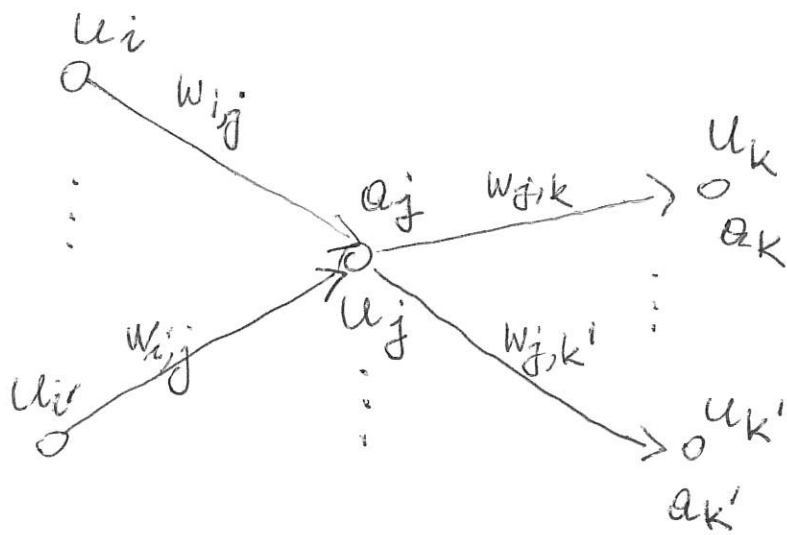
$$\frac{\partial a_k}{\partial w_{ij}} = \frac{\partial g(\text{in}_k)}{\partial w_{ij}} = g'(\text{in}_k) \cdot \frac{\partial \text{in}_k}{\partial w_{ij}} = \sum_j w_{j'k} \cdot a_j'$$

only $w_{j'k}$, $j'=j$ matters!

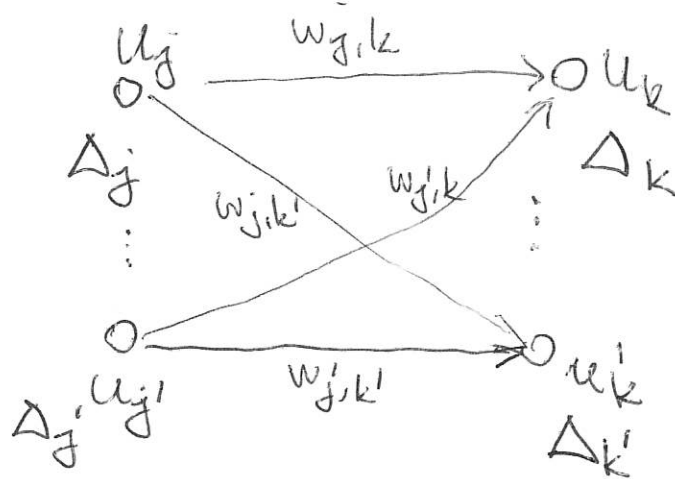
$$\frac{\partial a_j}{\partial w_{ij}} = \frac{\partial g(\text{in}_j)}{\partial w_{ij}} = g'(\text{in}_j) \cdot \frac{\partial \text{in}_j}{\partial w_{ij}} = \sum_i w_{i,j} \cdot a_i'$$

only $w_{i,j}$, $i=i$ matters

Multi-Layer Perceptron Learning



$$a_j = g(\text{in}_j) \quad a_k = g(\text{in}_k)$$



$$\Delta_j = g'(\text{in}_j) \cdot \sum_k w_{jk} \Delta_k$$

$$\Delta_k = \text{Err}_k \cdot g'(\text{in}_k)$$

Push back weighted errors